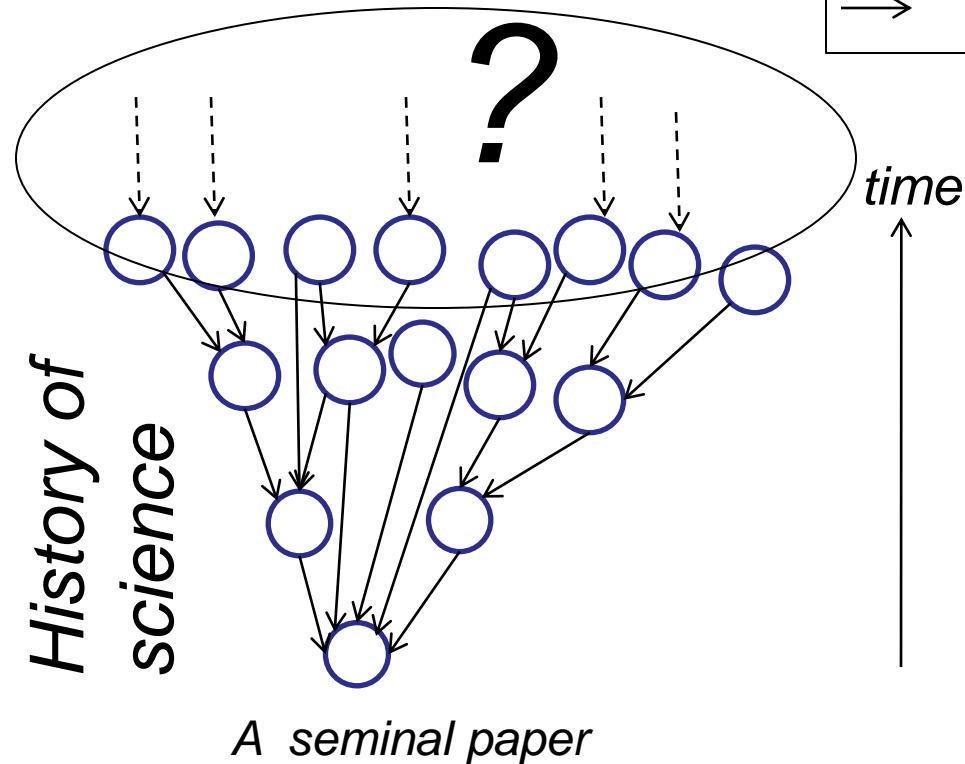




Motivation for studying citation dynamics

Research front



*Map of science shall be complemented by dynamics.
Both are obtained from citations.*

***Our goal is to establish a reliable model of citation dynamics,
preferably non-empirical one***



Citation Dynamics and Bass model of diffusion of innovations

Michael Golosovsky & **Sorin Solomon**

(experimental physics) *(physics of complexity)*

Racah Institute of Physics,

Hebrew University of Jerusalem, Israel

- *The model of citation dynamics of scientific papers*
- *Measurements to verify the model*
- *Discussion*

Our previous publications

M. Golosovsky and S. Solomon,

- *J. Stat. Phys. Special Issue Statistical Mechanics in Social Sciences 151 340 (2013);*
- *Phys. Rev. Lett. 109 098701 (2012)*
- *Eur. Phys. J. Special Topics 205 303 (2012)*



Models of Citation Dynamics

- *From the author's perspective*
- *From the paper's perspective*

Main idea: there are **two** kinds of citations

Generic models assuming two kinds of citations:

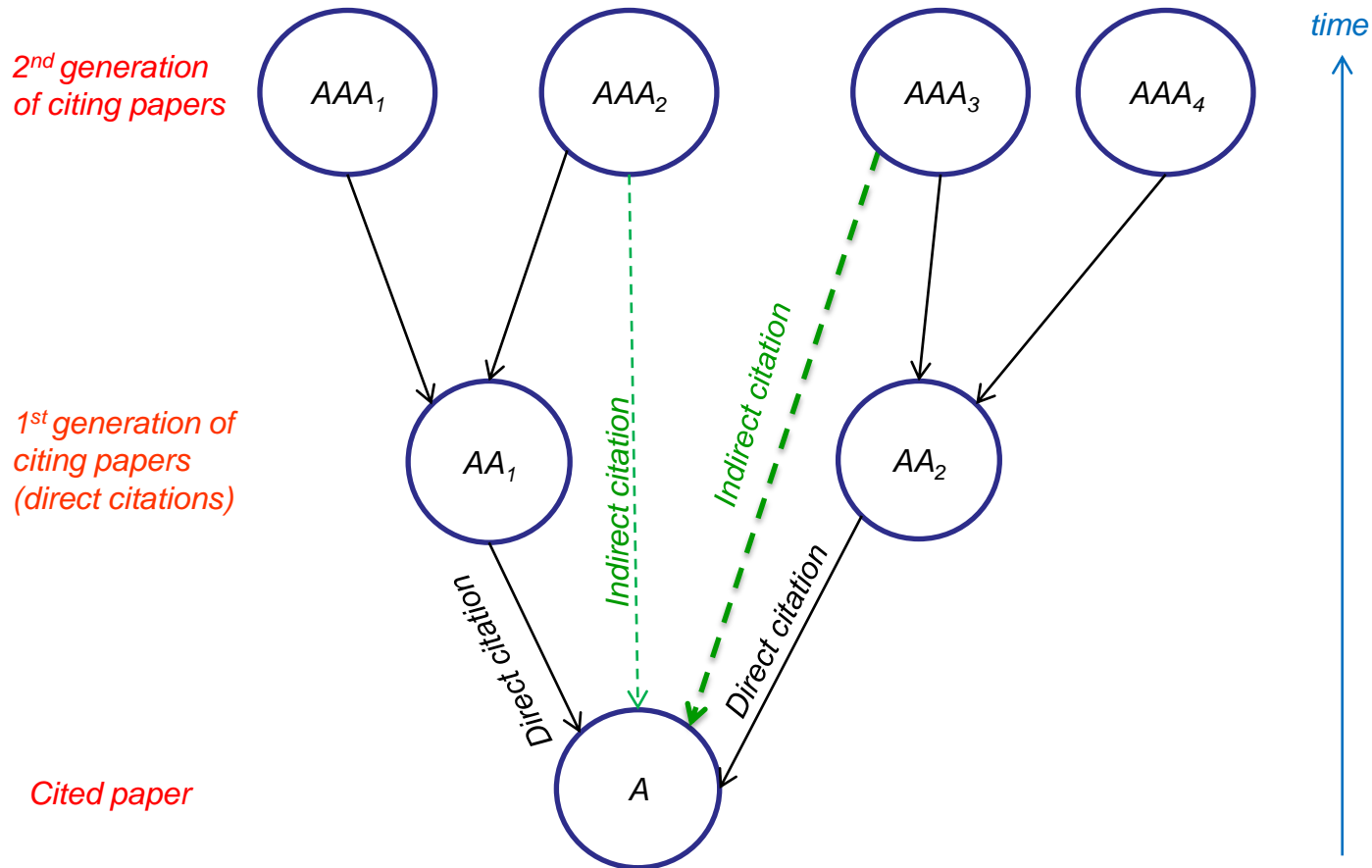
- *Recursive search – Vasquez (2001)*
- *Redirection - Krapivsky&Redner (2005)*
- *Link copying- Simkin&Roychowdhury (2007)*
- *Direct and indirect citations – Petersen, Presse&Dill (2009)*

*The overview of the models of citation dynamics-
Vitanov & Ausloos in*

“Models of Science Dynamics” ,A. Scharnhorst, K. Borner&P. Besselaar



Direct and indirect citations

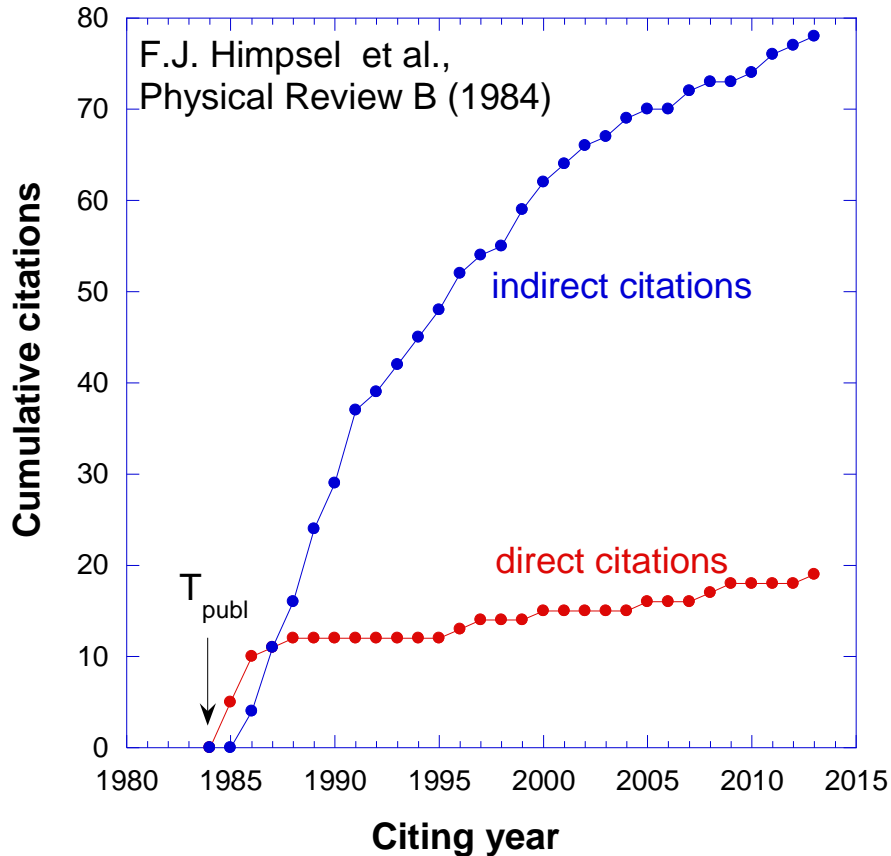


Direct citation: The citing author reads the paper and cites it
Indirect citation: The citing author reached to this paper through the reference list of another paper that he cites anyway

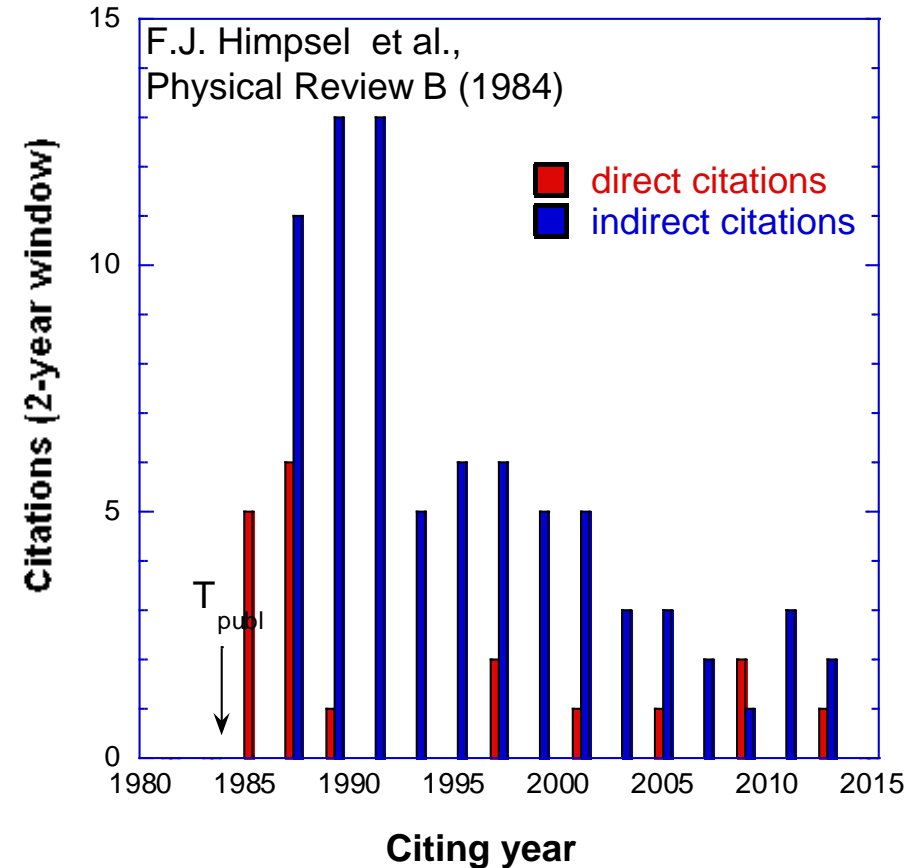


An example

Cumulative citations



Citation rate



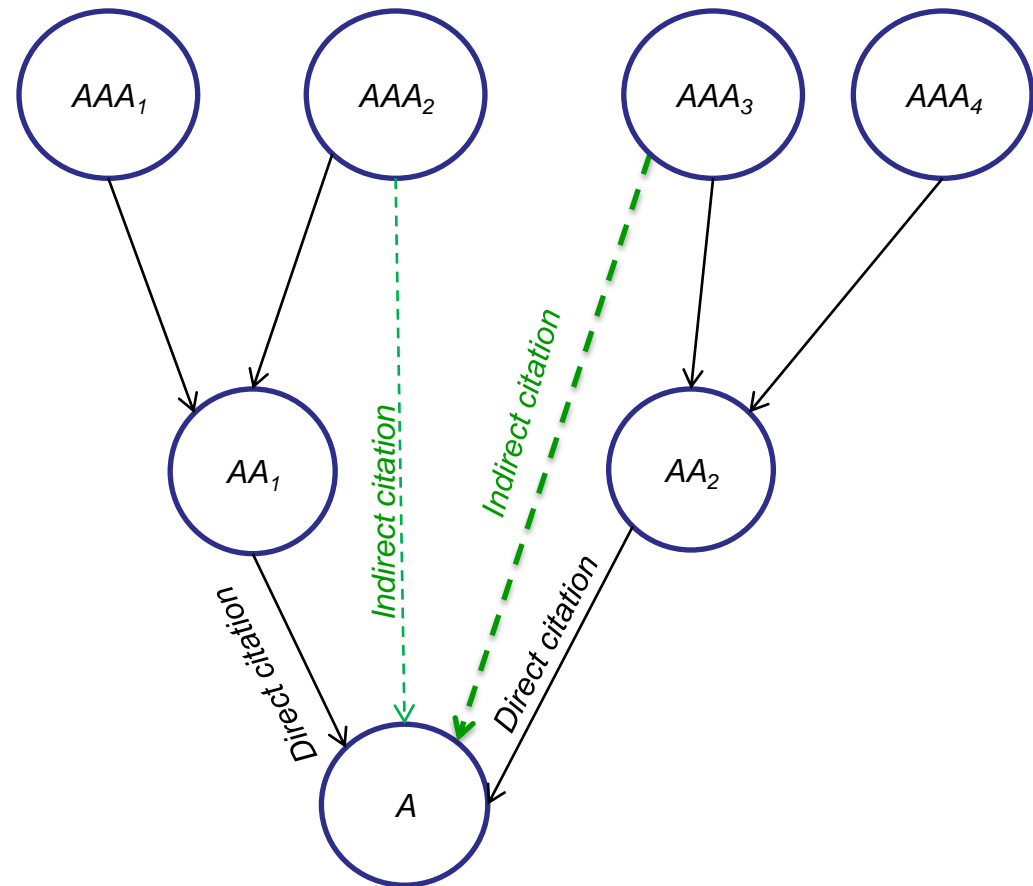
Direct citations appear immediately after publication and saturate after ~3-5 years.

Indirect citations start to grow after delay of ~1-2 years and come to saturation slowly (*if at all*)



The model and its context

- Population dynamics:
age-dependent birth-death model with immigration
- Epidemiology
SI (susceptible-infected) model
- Rumor propagation
- **Diffusion of innovations**
- **Marketing:**
product penetration into the market





Bass model of diffusion of innovations

F. Bass (1969)

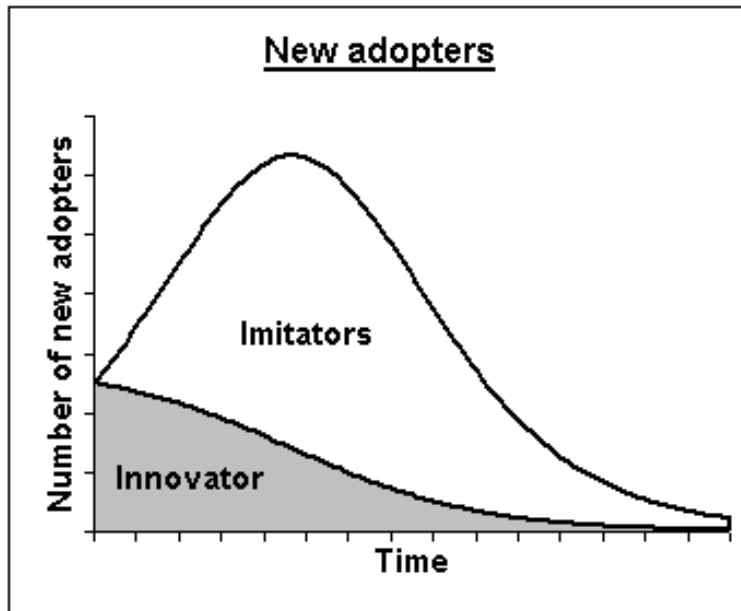
$$\frac{dN}{dt} = \left(p + \frac{q}{\bar{N}} N \right) \left(1 - \frac{N}{\bar{N}} \right)$$

N - total number of adopters

\bar{N} - number of potential adopters (market size)

p - coefficient of innovation

q - coefficient of imitation



*Innovators are reached by broadcasting
Imitators are reached by word-of-mouth*



Bass model of diffusion of innovations

Innovations

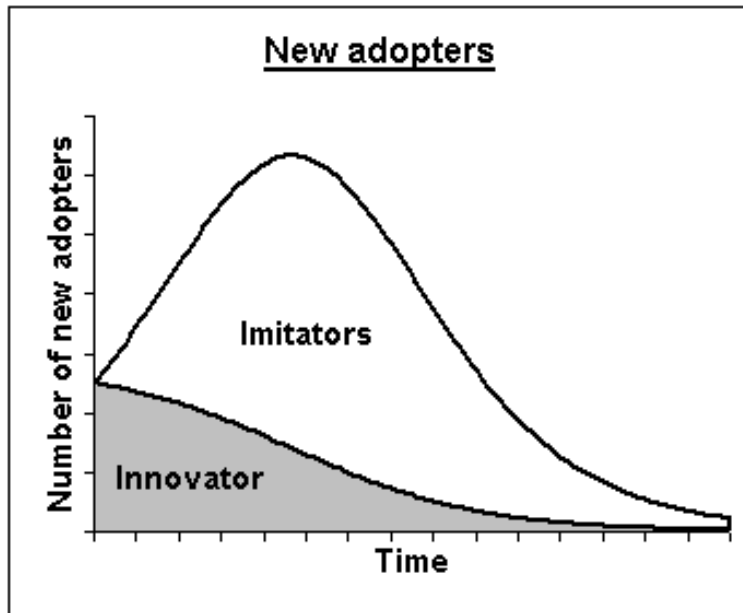
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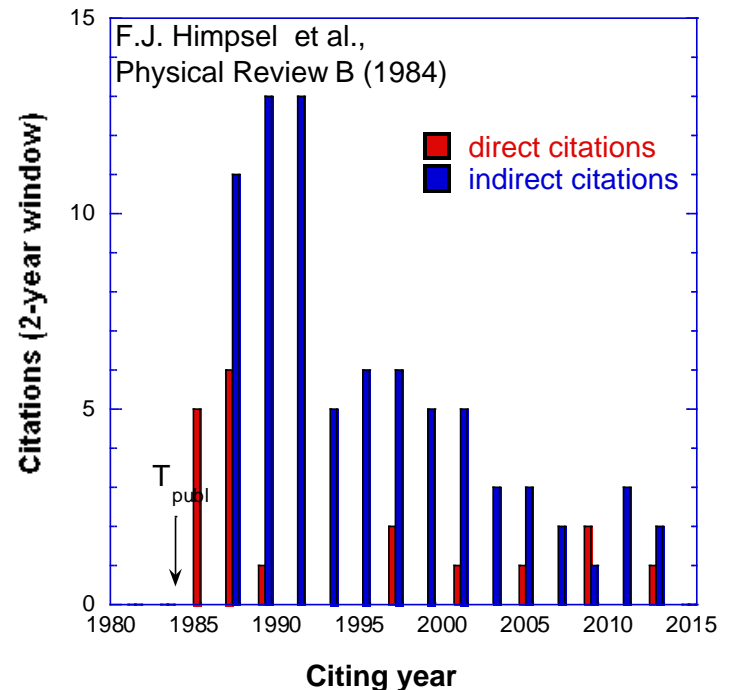


Citations

$$\frac{dk}{dt} = p(t) + \int_0^t q(t - \tau) \frac{dk}{d\tau} d\tau$$

Adopters = innovators & imitators

Citations = direct & indirect





Epidemic model: an application to the transmission of ideas

Goffman-Newill (1964)

Epidemiology- SI model

$$\frac{dS}{dt} = \mu - \beta IS$$

$$\frac{dI}{dt} = \nu + \beta IS$$

S – susceptible

I – infected

$$\text{if } S = \text{const} \text{ then } \frac{dI}{dt} = \nu + \beta SI$$

Citations

$$\frac{dk}{dt} = p(t) + \int_0^t q(k, t - \tau) \frac{dk}{d\tau} d\tau$$

Total
citations

Direct
citations

Indirect
citations

$$\text{if } q = \text{const} \text{ then } \frac{dk}{dt} = p(t) + qk$$

Total citations- infected

Direct citations- ν

Indirect citation – βIS



The model and the measurements

Self-exciting (non-Markovian) stochastic process

λ – latent citation rate :

$$\lambda = p(t) + \int_0^t q(t-\tau) \frac{dk}{d\tau} d\tau \longleftarrow \text{memory}$$

actual citations in the time window Δt follow a

Poisson process where $\Delta k = \lambda \Delta t$ and $P(\Delta k) = \frac{\lambda^{\Delta k}}{(\Delta k)!} e^{-\lambda}$

To apprehend the model we used ISI Web of Science and considered Physics papers published in 1984.

1st step: analysis of a small dataset of 36 papers

- *We measured direct and indirect citations separately*
- *Found functions $p(t)$ and $q(t-\tau)$*

2nd step: verification of the model using large data set of 40,195 papers

- *Verified parameters $p(t)$ and $q(t-\tau)$*
- *Verified that the noise is indeed Poissonian*



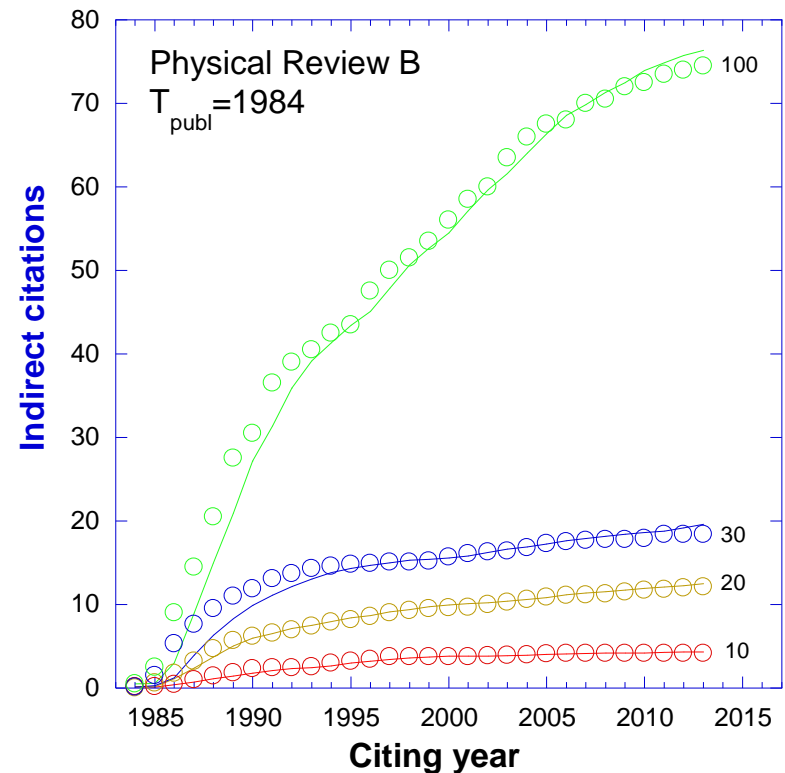
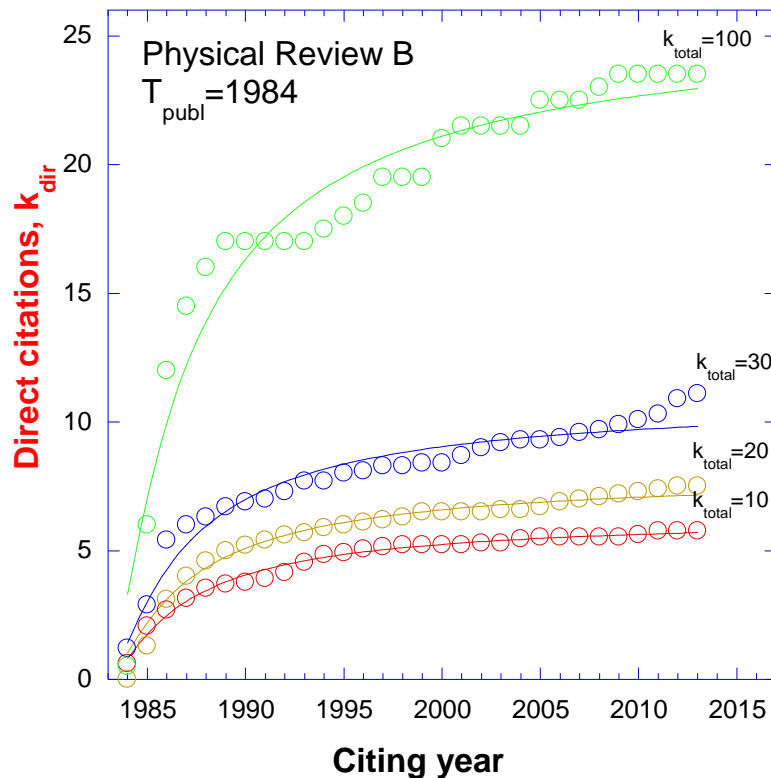
Comparison to the model

$$\frac{dk}{dt} = p(t) + \int_0^t q(t-\tau) \frac{dk}{d\tau} d\tau$$

$$p = p_0 e^{-\frac{3.4}{t+0.7}}$$

$$q = q_0 e^{-0.8(t-\tau)}$$

small dataset of 36 papers

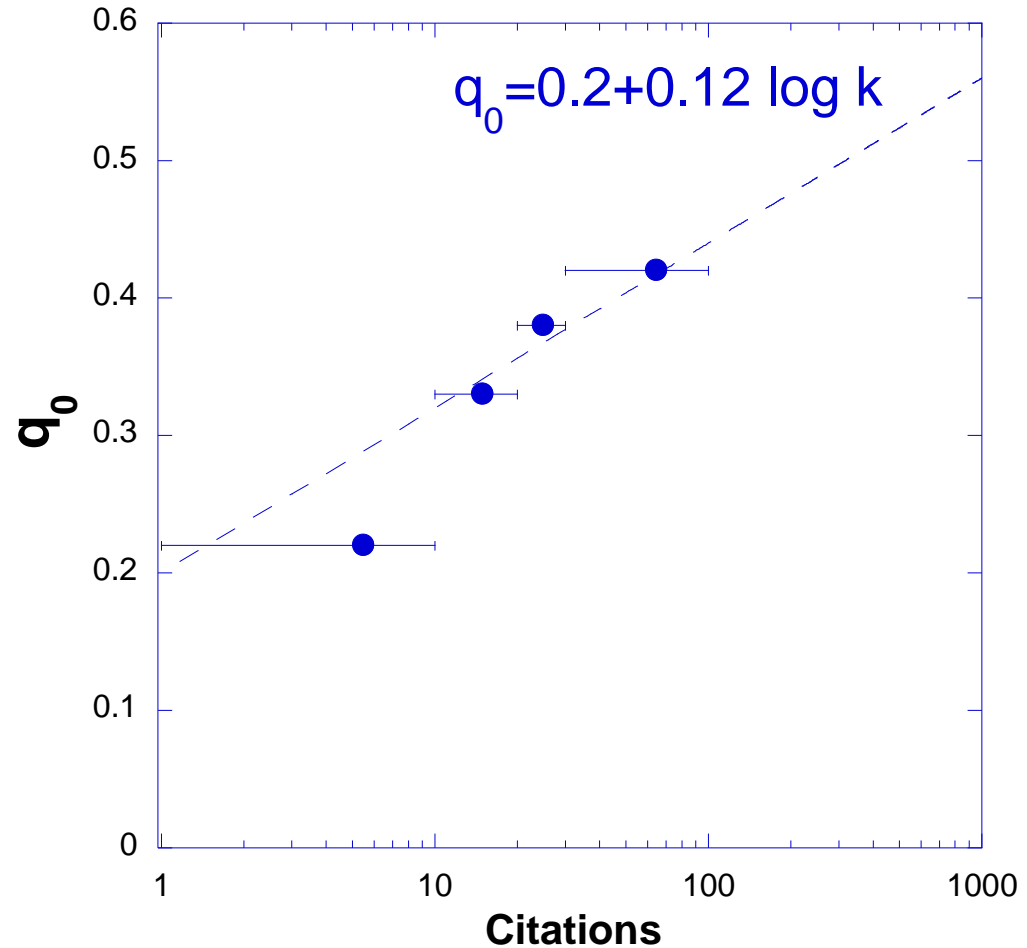




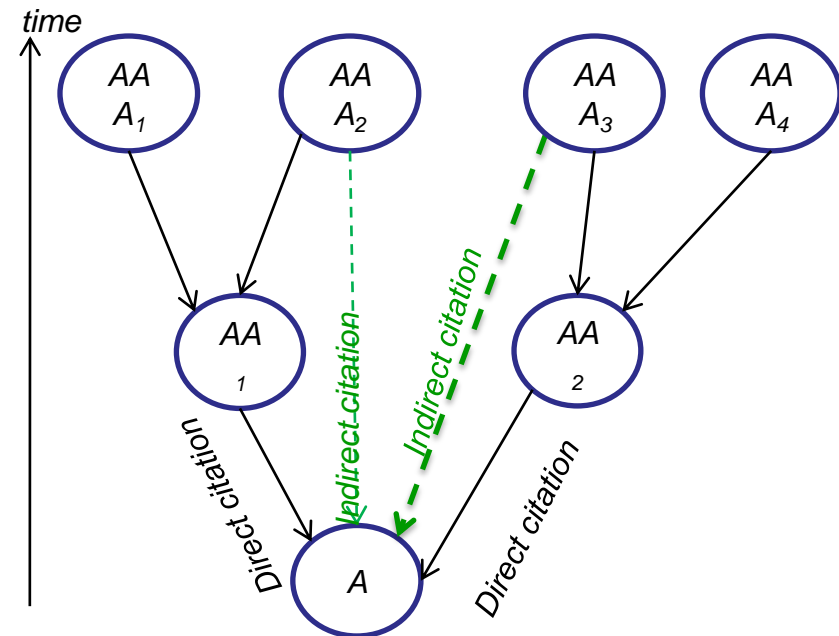
Analysis of results: nonlinearity

$$\frac{dk}{dt} = p(t) + \int_0^t q(k, t - \tau) \frac{dk}{d\tau} d\tau$$

$p = p_0 e^{-\frac{3.4}{t+0.7}}$; p_0 - initial conditions
 $q = q_0 e^{-0.8(t-\tau)}$; q_0 depends on k !?

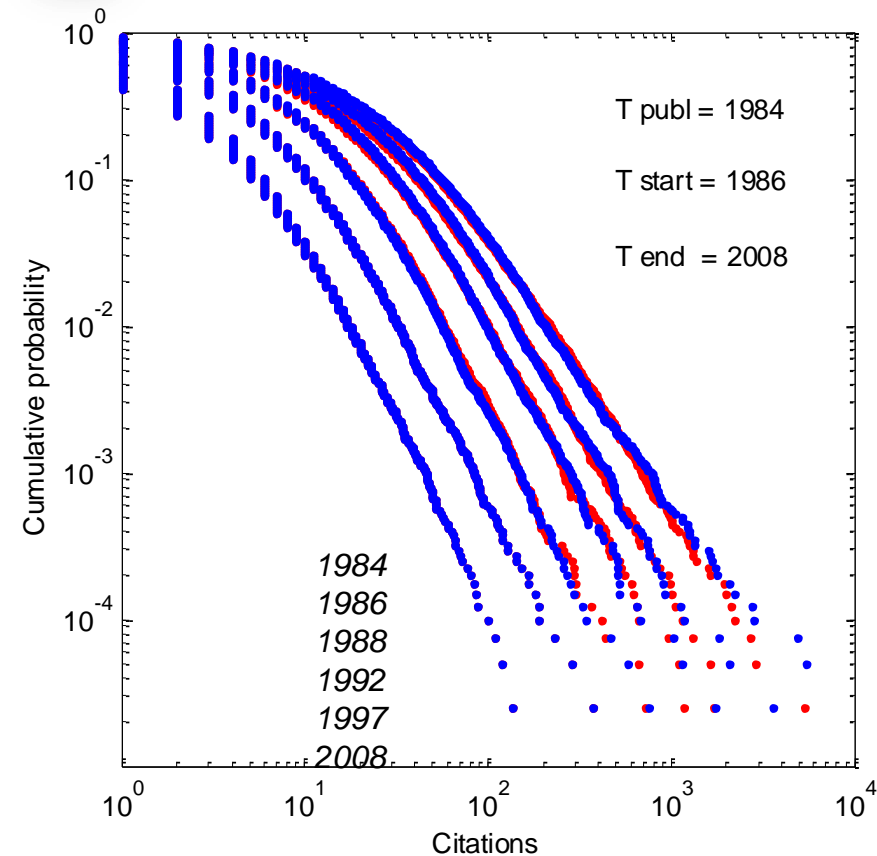


The memory is short- only 1.5-2 years



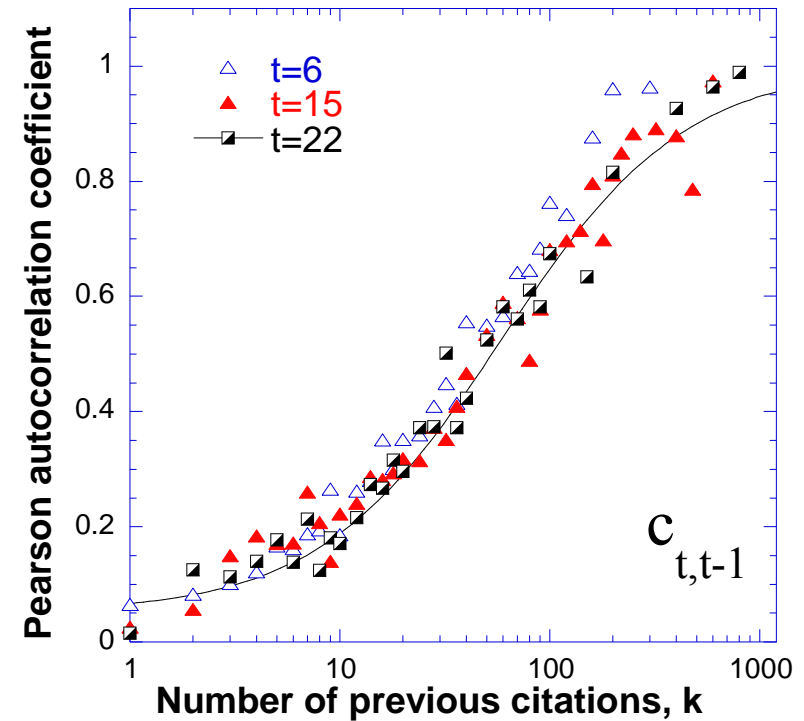


Verification of the model



Cumulative citation distributions to 40,195 Physics papers published in 1984. The model takes the data for 1984, 1985, and 1986 as initial conditions and calculates citations further on.

Blue circles- model, red circles- data



Pearson **autocorrelation** coefficient.
It captures memory effect.

large dataset of 40,195 papers



Analysis of the model

$$P(\Delta k) = \frac{\lambda^{\Delta k}}{(\Delta k)!} e^{-\lambda}$$

Latent citation rate

$$\lambda = p(t) + \int_0^t q(k, t - \tau) \frac{dk}{d\tau} d\tau$$

positive feedback due to nonlinearity + self-excitation

The theoretical models completely missed the nonlinearity

“There are more things in heaven and earth, Horatio,
Than are dreamt of in your philosophy.”

-William Shakespeare, *Hamlet*



Consequences of nonlinearity

- *Citation distributions are non-stationary*
- *Runaways*

For simplicity , consider impulse response

$$\frac{dk}{dt} = P\delta(t) + \int_0^t q_0 e^{-\beta(t-\tau)} \frac{dk}{d\tau} d\tau$$

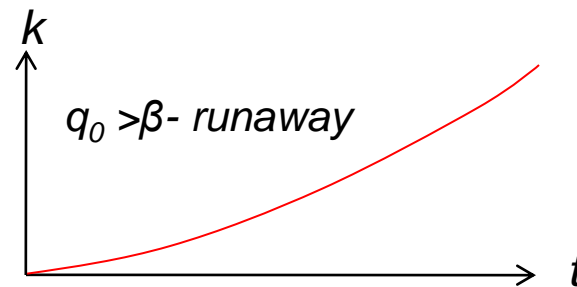
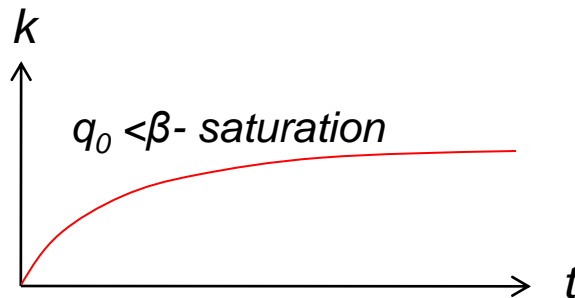
solution : $\frac{dk}{dt} = Pq_0 e^{-(\beta-q_0)t}$

$$k = P \left[1 + \frac{q_0}{\beta - q_0} \left(1 - e^{-(\beta-q_0)t} \right) \right]$$

$q_0 = \beta$ - branching (tipping) point

since q_0 increases with k ,
highly - cited papers
can pass tipping point
and become runaways

Branching process
Citation cascades
 q_0/β – reproduction number



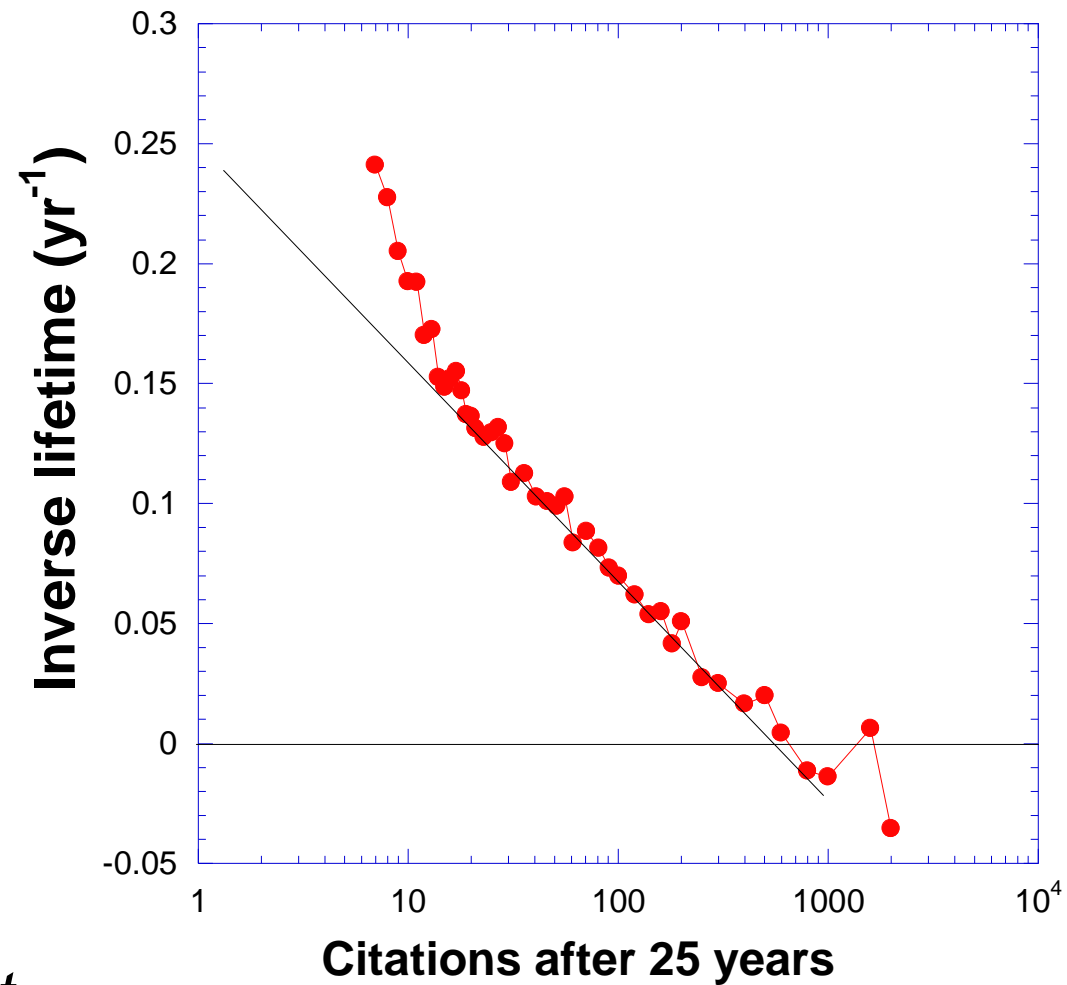


Runaways

$$\frac{dk}{dt} = Pq_0 e^{-(\beta - q_0)t}$$

$(\beta - q_0)$ – inverse lifetime

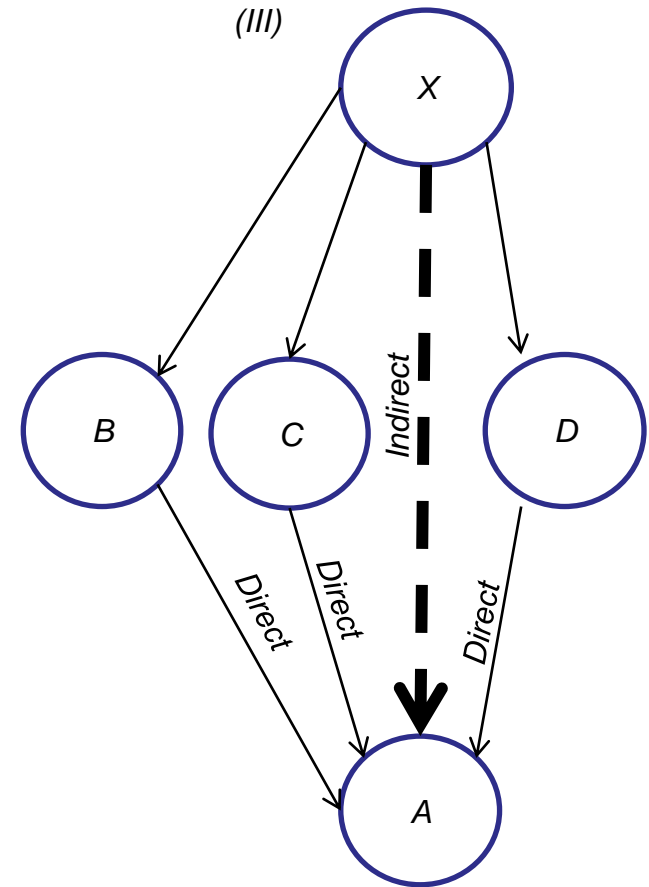
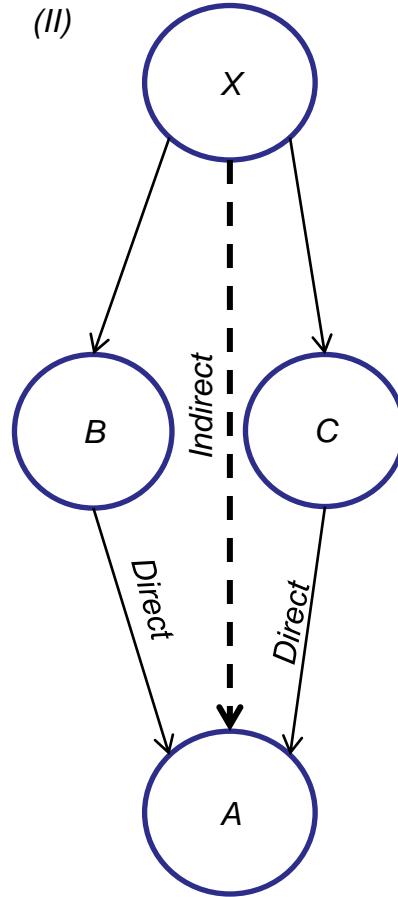
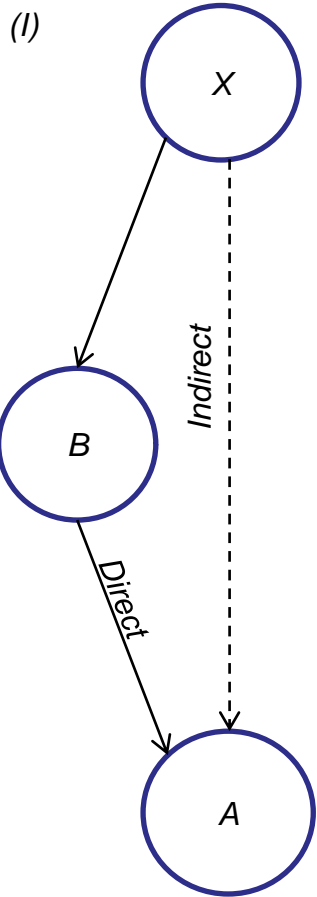
$$q_0 = 0.2 + 0.12 \log k$$



*Not only “rich get richer” but
Rich live longer!*



What is the source of nonlinearity? Look at network motifs

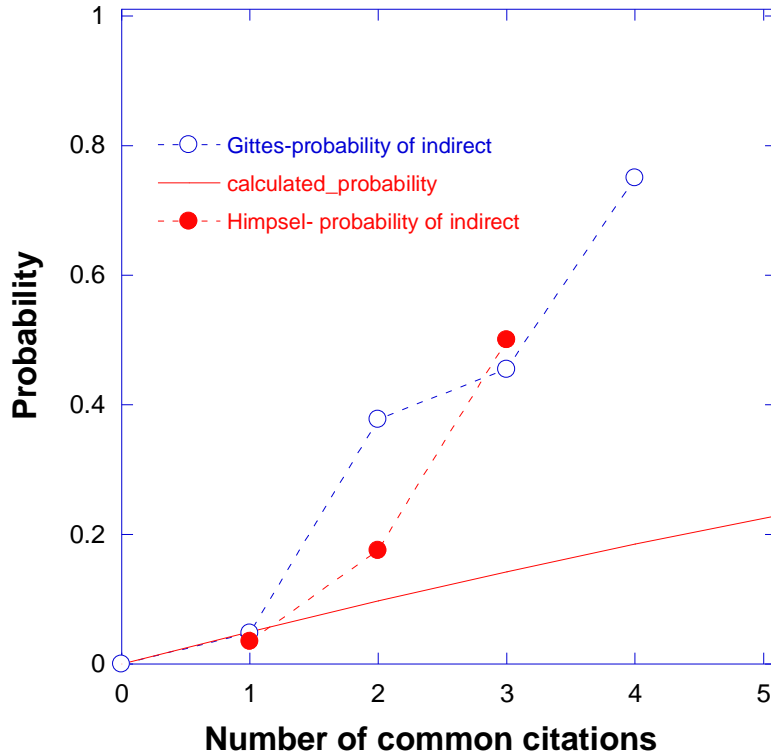


$$3q^{III}_{indirect} > 2q^{II}_{indirect} > q^I_{indirect}$$

Homophily? Peer-to-peer influence?

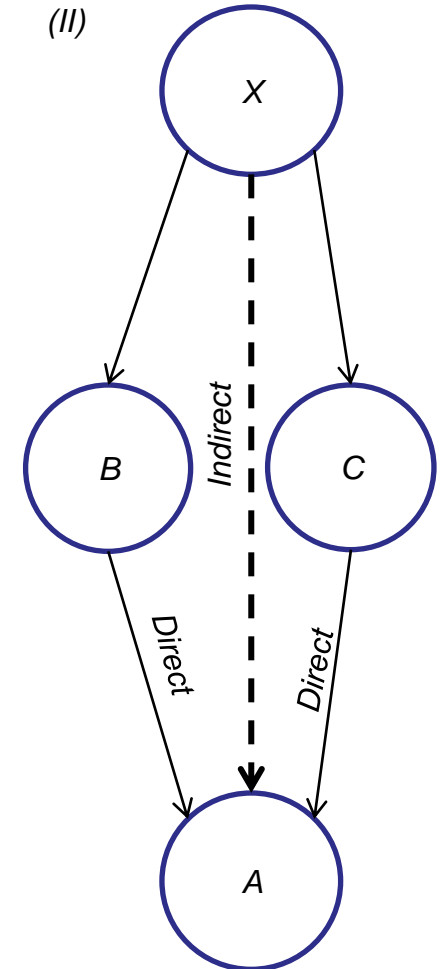


Multipath interference



Probability of indirect citations in dependence on the number of common direct citations. Continuous line shows linear approximation (no multipath interference).

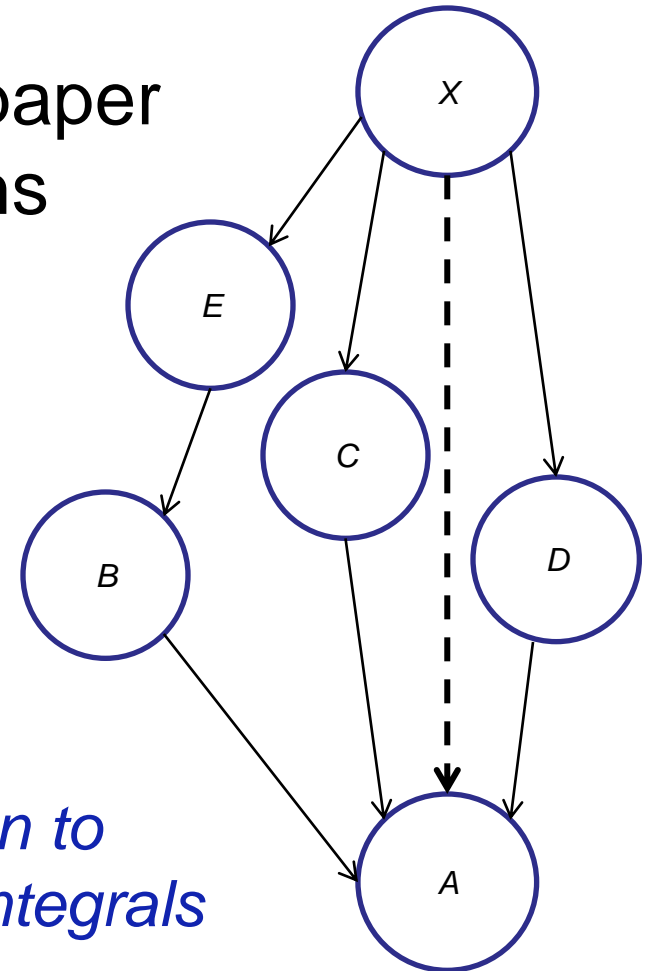
(II)





The probability that paper X cites paper A is the weighted sum over all paths leading from X to A

Pathways are important!



Physicists can appreciate possible relation to multipath interference or Feynman path integrals



Conclusions

- Microscopic model of citation dynamics based on nonlinear self-exciting process
- Verification of the model
- Deep analogy between citation dynamics and diffusion of innovations/products:

Citation dynamics of a paper captures penetration to market of ideas: broadcasting (direct) and word-of-mouth (indirect) mechanisms are clearly seen



Future plans and applications

- Forecasting

prediction of the future citation history of a given set of papers

- impact factor of a journal

- h-index of a researcher

- Research frontiers

Early identification of important papers



Relation to previous talks

Memory, non-Markovian processes- Martin Rosvall, Marton Karsai, Renaud Lambiotte, Ingo Scholtes

Economic analogies, Knowledge diffusion- Bruno Goncalvez

*Runaways (in the context of institutions) –*Nikolay Vitanov

h-index- and how to affect/predict it- Serge Galam, Raj Kumar Pan

Stochastic process, autocorrelation/autocovariance – Oleg Yordanov

Homophily- Sanja Scepanovic

Pathways- Renaud Lambiotte

Predictability- Ingo Scholtes